

Calc 2

Area of a Looped Limacon

Not Using Symmetry

Normal Area of Everything

$$\frac{1}{2} \int_0^{2\pi} r^2 d\theta - \frac{1}{2} \int_{\text{start of loop}}^{\text{end of loop using reference angle}} r^2 d\theta$$

Area In Between

$$\frac{1}{2} \int_0^{2\pi} r^2 d\theta - 2 \cdot \frac{1}{2} \int_{\text{start of loop}}^{\text{end of loop using reference angle}} r^2 d\theta$$

Area of Inner Loop

$$\frac{1}{2} \int_{\text{start of loop}}^{\text{end of loop using reference angle}} r^2 d\theta$$

Using Symmetry

Normal Area of Everything

$$2 \cdot \frac{1}{2} \int_{0 \text{ or neg beginning of loop}}^{\text{start of loop}} r^2 d\theta$$

Area In Between

$$2 \cdot \frac{1}{2} \int_{0 \text{ or neg beginning of loop}}^{\text{start of loop}} r^2 d\theta - 2 \cdot \frac{1}{2} \int_{\text{start of loop}}^{\text{halfway pt of loop}} r^2 d\theta$$

Area of Inner Loop

$$2 \cdot \frac{1}{2} \int_{\text{start of loop}}^{\text{halfway point of loop}} r^2 d\theta$$